

A Computational Investigation of Redistricting Using Simulated Annealing

Vjatsešlav Antoškina¹ and Benson K. Muite²

Abstract

Political redistricting is done to ensure fair selection of electoral representatives. It can be formulated as a combinatorial optimization problem. The effectiveness of parallel computing to more effectively search the solution space is examined in specially designed test cases where the optimal solution is known.

Introduction

Gerrymandering is the process of creating electoral districts that favor election of a particular candidate or party. In some countries the redistricting process is done by elected members, who can perform the redistricting process to favor re-election of the incumbent and reduce the competitiveness of the electoral process.

One way to do redistricting for American congressional districts is by assigning census blocks or counties to particular congressional districts. In doing so, the main principles to be followed are [1, 6]:

- Approximately equal number of voters per congressional district
- Compact congressional districts
- Hole free congressional districts
- Where possible competitive congressional districts with as close to even partisan support

To capture these principles, one defines a global objective function to capture the effectiveness of a particular redistricting plan. An optimization routine is then used to find a good redistricting plan.

Previous Work

- PEAR (Parallel evolutionary algorithm for redistricting) is a recent work that combines parallel computing with genetic evolution to find good redistricting plans [6, 7].
- Earlier influential work includes BARD (Better automated redistricting) - open source R package for computational redistricting [1].
- Human input will still be needed for redistricting [2].

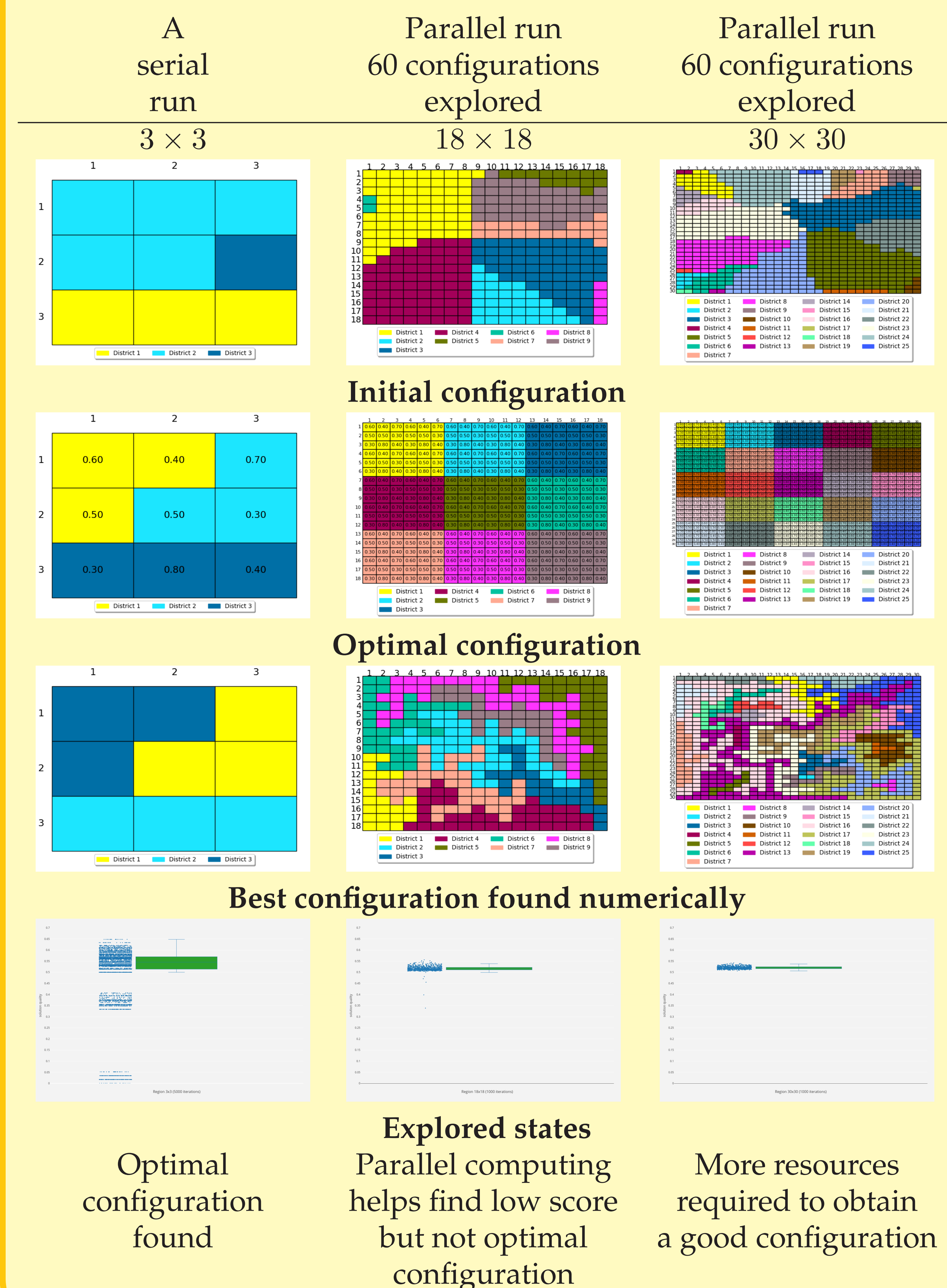
Research Question

If the objective function has been correctly chosen, what is the amount of computational work that is required to obtain the best redistricting plan(s)?

Method

In this study simulated annealing was used to find good solutions. An initial configuration was chosen that satisfied the contiguity and hole free constraints. This was then evolved for between 1000 to 5000 iterations. The configuration with the best score was recorded. Parallelization involved running multiple independent initial conditions in an ensemble (without interaction). More details and source code are in [3].

Results



Summary

- Initial results demonstrate parallelization can help in searching a wider space to obtain good redistricting plans.
- The example programs are written in Python and do not have optimal computational complexity but should be easy to update and experiment with.
- As found in [4] for states with a small number of congressional districts (such as Idaho and Oregon), computers can obtain good redistricting plans.
- An enumeration of the number of possible redistricting plans would be very helpful in determining appropriate computational resources to use to give a high probability of finding the optimal redistricting plan.
- It would be interesting to use genetic evolution algorithms in cases where the optimal redistricting plan is known to determine their effectiveness in real world use.

References

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Contact

Institute of Computer Science, University of Tartu, Tartu, Estonia

[1] vjatseslav.antoskin@ut.ee [2] benson.muite@ut.ee